

slln-lemma1^{11,40}

$\forall p:\text{FinProbSpace}, f:(\mathbb{N} \rightarrow \mathbb{N}), X:(n:\mathbb{N} \rightarrow \text{RandomVariable}(p;f(n))), s, k:\mathbb{Q}.$
 $(\forall n:\mathbb{N}, i:\{0..n^-\}. f(i) < f(n))$
 $\Rightarrow (\forall n:\mathbb{N}.$
 $\quad \text{E}(f(n);X(n)) = 0 \in \mathbb{Q}$
 $\quad \& \text{E}(f(n);(x.x * x) \circ X(n)) = s$
 $\quad \& \text{E}(f(n);(x.(x * x) * x * x) \circ X(n)) = k)$
 $\Rightarrow (\forall n:\mathbb{N}, i:\{0..n^-\}. \text{rv-disjoint}(p;f(n);X(i);X(n)))$
 $\Rightarrow (\exists B:\mathbb{Q}$
 $\quad (0 \leq B \ \& \ (\forall n:\mathbb{N}. \text{E}(f(n);(x.(x * x) * x * x) \circ \text{rv-partial-sum}(n;i.X(i))) \leq B * n * n)))$